Incentives and Compensation Schemes: An Experimental Study

Marina Agranov† and Chloe Tergiman‡

November 2011

Abstract

When the performances of agents are correlated (because of a common random component) contracts that use information on both the relative and absolute performance of agents theoretically outperform rank-order tournaments and piece-rate schemes. Although the theoretical advantage of such contracts has long been noticed in the literature, the empirical papers that study this question have produced mixed results. Using a controlled laboratory experiment, we shed light on the performance of these contracts. We focus on the simplest version of such a contract: the Relative Piece-Rate (RPR) and compare its performance with that of tournaments and piece-rate schemes. We find that when the RPRs are imposed on the agents, they exert higher effort levels and give the principal (weakly) higher profits than tournament and piece-rate contracts. Second, we find that agents have little aversion to self-select into the RPR scheme when other alternatives are available. In our paper we fix the environment agents face and vary only their wage scheme. Our results support the theoretical predictions and suggest that principals can benefit from using RPR schemes in places where piece-rate and tournament contracts would otherwise be used.

Keywords: incentives, compensation schemes, laboratory experiments, moral-hazard.

*We are particularly indebted to Guillaume Frechette and also Andrew Schotter for the time and guidance they generously gave us at every stage of this project. We thank Heski Bar-Isaac, Alessandro Lizzeri, Viktor Raskin, Mikael Rechtsman and Ariel Rubinstein for constructive criticism. We also thank John Duffy, Charlie Holt, Tim Salmon and Lise Vesterlund for useful discussions and comments. The Center for Experimental Social Science at New York University provided us with the facilities and funds to conduct our experiments. We would also like to thank the participants and organizers of the following conferences: the French Economic Association on Behavioral Economics and Experiments in Lyon, the University of Amsterdam CREED, the World ESA meeting in Rome, and the North American ESA meeting in Arizona.

†Caltech and CESS
‡University of British Columbia and CESS


1 Introduction

When the performances of risk-averse agents are correlated (because of a common random component), using relative performance information can improve the trade-off between incentives and risk-sharing. For example, when the common shock is a big part of the uncertainty, the optimal rank-order tournament (T), which pays a higher prize to the agent that produced the higher output, guarantees the principal a higher expected profit than the optimal independent piece-rate contract (IPR), in which agents are paid linearly based only on their absolute performance. However, even when tournaments theoretically outperform piece-rate contracts, they are “informationally quite wasteful if performance levels of agents can be measured cardinally rather than ordinally”, (Holmstrom (1982)). Indeed, if the exact outputs of agents are observable, there is a better way of using this information in contract design.

The theoretical advantage of contracts that make use of both relative and absolute performance information of agents has been long known in the literature. However, the empirical studies that investigate the efficacy of these contracts in the labor markets have produced mixed results. Much of this literature uses data from CEO pay and the results are far from being clear (summarized in section 1.1). In this paper we aim to complement the empirical literature by conducting a controlled laboratory experiment, which evaluates the performance of such a contract. For simplicity and in line with the theoretical literature\(^1\), we concentrate on a contract that is linear in both agents’ performance. We call it the Relative Piece-Rate (RPR) scheme. In the RPR, each agent receives payment in proportion to his output as in the IPR scheme, but he is also penalized in a linear way for every unit of output produced by the other agent. We compare the RPR scheme with Tournaments and IPRs because they are often used in practice\(^2\) and, hence, form a natural baseline for comparison.

There are several reasons why a laboratory experiment is a useful approach in the


\(^2\)Standard examples of rank-order tournaments include promotion tournaments for managers, bonuses for salespeople at the end of the year, a tournament for limited number of tenure positions that assistant professors compete for etc. The IPR is often used in industries such as fruit picking or when people are paid on commission. The percentage of workers who receive their compensation in the form of bonuses or piece-rates is substantial. Lemieux, MacLeod and Parent (2009) report that the overall fraction is about 40%, and within sales and services the fraction of employees receiving their pay this way is about 75% and 20%, respectively.
current situation. We are interested in testing the performance of the RPR scheme and comparing it with the performance of the Tournament and IPR schemes. The key advantage of using the lab to answer this question is the ability to control many aspects of the environment, which is necessary for the comparison to be fair and adequate. These aspects are often impossible to observe or infer from labor market data. Moreover, while empirical data is rich, it often reflects a variety of environmental factors that affect the performance of the agents and are extremely hard to separate out. The lab environment is clean and gives the experimenter the freedom to fix all the parameters of the environment and vary only the scheme imposed on the agents. This allows for a rigorous comparison across wage scheme designs. Over the past 20 years, laboratory experiments have proven useful in understanding many important questions posed by labor economics (see survey by Charness and Kuhn (2010)). However, as far as we know, we are the first ones to try to resolve the conflicting empirical evidence regarding the RPR-like schemes using a laboratory experiment.

One important and unique feature of our experimental design is that we fix the environment that the principal faces, and test the performance of the RPR, T and IPR contracts with the optimal parameters that are determined by this environment. The environment we chose is standard in the literature: it represents one example of a broad class of environments, in which according to the theory RPR performs better than T and IPR contracts. Our choice to fix the environment is in sharp contrast with past experimental papers. Indeed, up to now, the literature has primarily focused on whether agents targeted the effort prediction of a wage scheme. Put differently, other studies chose the parameters of the wage scheme so that that the predicted effort levels were the same across wage schemes. This means that the prior literature aimed to compare how well schemes could elicit a fixed (identical) effort level. This was without regards to whether the coefficients in these wage schemes (1) corresponded to the same environment, or (2) were optimal given an environment. In fact, if the experimenter holds the effort level prediction constant across wage schemes, then the parameters in those wage schemes cannot both be optimal and correspond to the same environment. To our knowledge,

---

3 See section 3 for the formal description of the environment and conditions under which the RPR contract delivers higher effort levels of agents and higher expected profits to the principal than the IPR and the T contracts.

we are the first to keep the environment constant across wage schemes. We can there-
fore compare wage schemes from the view point of a profit-maximizing principal facing
a particular environment. In other words, while the results from these past experiments
provide insight into subjects’ behavior, they cannot address the question “How should a
principal, facing a specific environment, choose to pay his employees?,” which is the main
focus of this paper.

We designed two experiments. The purpose of Experiment 1 was to study how well
the RPR scheme performs relative to the IPR and T, both in terms of the agents’ efforts
and of the profits earned by the principal when a wage scheme is imposed on the subjects.
The results from Experiment 1 support the main theoretical predictions. The profits of
the principal under the optimal RPR scheme are (weakly) higher than in the T and IPR.\(^5\)
Also, workers exert strictly higher efforts under the optimal RPR scheme when compared
to the optimal T and IPR schemes. This is true when these contracts are exogenously
imposed on agents. However, it is possible that people have an intrinsic aversion to
some types of contracts, and if presented with the choice of several contracts, would not
self-select into the RPR.

In Experiment 2 we allow (new) subjects to self-select into either compensation
scheme. The purpose of Experiment 2 was to evaluate whether or not subjects exhibited
certain biases against or in favor of the RPR (or any other scheme), and whether these
biases were enforced or mitigated by experience. With our design, subjects should be
indifferent between all three wage schemes in terms of their expected utility. Therefore,
if they like or dislike one scheme more than the other it would be for reasons that are
outside of utility maximization. The results of Experiment 2 indicate that subjects do not
seem averse to the RPR. On the contrary, not only do subjects choose to participate in
the RPR over the T and IPR before they have any experience, but they remain with the
RPR and even switch to it after they have gained experience in all three wage schemes.\(^6\)

All together, our findings from Experiment 1 and Experiment 2 confirm that the RPR

\(^5\)The RPR always generates higher profits for the principal than the T contract. With respect to the
IPR contract, in one environment RPR gives strictly higher profits and in the other, the RPR and IPR
are “tied.”

\(^6\)In Experiment 2, we described all three wage schemes to the subjects. They then chose one wage
scheme to participate in. After they participated in that scheme, subjects were asked to participate in
all three wage schemes. After they gained experience in all three wage schemes, they were again offered
the choice of which payment scheme to participate in.
scheme outperforms T and IPR schemes and suggest that a principal could significantly increase his profits with a frequent use of RPR in place of IPRs or Ts.

The rest of the paper is organized as follows. The literature review is in Section 2. In Section 3, we describe the environment and state the theoretical results. The design and results from Experiment 1 are in Section 4. Experiment 2 is described in Section 5. We discuss the use of RPR schemes in practice in Section 6. Finally, Section 7 concludes.

2 Related literature

The early theoretical work on the performance of piece-rate contracts versus rank-order tournaments includes Lazear and Rosen (1981), Green and Stokey (1983) and Nalebuff and Stiglitz (1983). Later on, Holmstrom (1982) and Mookherjee (1984) studied the conditions under which relative performance contracts (not restricted to tournaments) perform better than independent contracts. Since then, there has been a lot of theoretical work in agency theory that has investigated the relative performance of contracts under different circumstances (see, for example, Meyer and Vickers (1987), Holmstrom and Milgrom (1991) and Levitt (1995)). More directly related to the present paper is Tsoulouhas (2010) that compares tournaments, piece-rates and “hybrid” tournaments that resemble our RPR scheme in a theoretical framework involving n players.7

While compelling theoretical arguments can be made in favor of relative performance evaluation schemes, empirical studies that assess their effectiveness has produced mixed results: some studies document that CEO’s pay is negatively related to industry performance (see Gibbons-Murphy (1990) and Janakiraman et al. (1992)); other studies show that relative performance is not an important source of managers’ contracts (see Jensen-Murphy (1990), Barro-Barro (1990) and Aggrawal-Samwick (1999)); while others find that CEO’s compensation increases with industry performance (see Joh (1999)) or that CEO’s dismissals are more likely when the industry is doing poorly (see Jenter-Kanaan (2006)), which is at odds with the idea of the relative performance evaluation.8

---

7 In Tsoulouhas (2010), in a tournament agents receive a bonus dependent on how much better they do than the average in addition to a flat payment. The weights on absolute and average group performance are equal in a standard tournament, whereas they are unequal under a “hybrid” tournament.

8 Knoeber (1989), Knoeber and Thurman (1994 and 1995) have studied these types of schemes in the context of the broiler chicken industry and find support for the these types of schemes.
The experimental literature that tests the behavioral performance of various incentive schemes consists of both laboratory and field studies. Among the laboratory studies are Bull, Schotter and Weigelt (1987), Harbring and Irlenbusch (2003), van Dijk, Sonnemans, and van Winden (2001) and Wu, Roe and Sporleder (2006). A consistent result in these experiments is that IPR schemes do well at eliciting the theoretically predicted level of effort, whereas tournament contracts have varied results.\textsuperscript{9} While our focus is mainly on the performance of the RPR scheme, consistent with the existing literature, our findings indicate that the tournament contract does not perform always as theory predicts. More precisely, our results indicate that tournament scheme performs the worst (compared to IPR and RPR) when the common uncertainty is relatively large, which is exactly when it has theoretical advantages.

In terms of field experiments, the closest work to ours is Bandiera, Barankay and Rasul (2005) who conducted a field experiment in a fruit picking plant and compared three wage schemes: an individual piece-rate, a relative compensation scheme where individual pay and group performance are negatively correlated, and a relative compensation scheme where individual pay and group performance are positively correlated (group incentives). The authors observe that effort is higher under the individual pay schemes. However, the parameters of the wage schemes used in this field experiment were not necessarily optimal, and it is unclear what the results would have been if this had been the case. While conducting an experiment in the field has its obvious and important advantages, the laboratory experiment has a useful contribution to our understanding of the effect of incentives on workers’ behavior by controlling all parameters of the environment.

\textsuperscript{9} Bull, Schotter and Weigelt (1987), for example, report that subjects respond on target to the different IPR schemes, but for some tournaments their effort choices are off with subjects choosing extremely low effort levels (a behavior associated with “dropping out”), which they do not do in the IPR schemes. Harbring and Irlenbusch (2003) focus on the effect of tournament design on effort levels. They do not make point predictions but study how well subjects understand in which direction their effort should go to maximize their payoff when faced with a different tournament structure. Wu, Roe and Sporleder (2006) find that for a fixed total uncertainty, increasing the relative importance of the common shock results in subjects choosing below equilibrium effort levels.
3 Theory

In this section we describe the environment and derive the optimal parameters of our three wage schemes: the relative piece-rate (RPR), the independent piece-rate (IPR) and the tournament (T). We then show that the relative performance of these schemes depends on the characteristics of the environment; however, the RPR always dominates both the IPR and T schemes in terms of the principal’s profits and effort levels of agents.

Consider a standard moral-hazard setting à la Holmstrom (1979). A risk-neutral principal hires 2 agents (i and j) to produce output. The principal’s profit consists of the total output produced by workers minus the cost of hiring them. The output of an agent i has an additive structure: \( y_i = e_i + \epsilon_i + \eta \), where \( e_i \) is the effort level privately chosen by agent i, \( \epsilon_i \) is her private production shock and \( \eta \) is a common production shock that affects both agents equally. The effort levels of agents are not observable and therefore not contractible. The principal observes only the output produced by each agent.

Agents are risk-averse. The utility of agents i is \( u(x) = -e^{-rx} \) where \( r \) represents the coefficient of absolute risk aversion. Effort is costly and the cost function associated with effort \( e_i \) is given by \( (e_i)^2 \). The private shocks \( \epsilon_i \) and \( \epsilon_j \) are independently drawn from \( U[-A,A] \) and the common shock \( \eta \) is drawn from \( U[-B,B] \).

There are three possible wage schemes that the principal can employ:

- **RPR scheme**: Agent i gets wage \( i = \alpha + \beta \cdot y_i + \gamma \cdot y_j \)
- **IPR scheme**: Agent i gets wage \( i = \alpha' + \beta' \cdot y_i \)
- **Tournament scheme**: The agent with the highest output wins a big prize \( W_1 \), the other agent gets a small prize \( W_2 \).

The principal chooses the parameters for each of the schemes to maximize his expected profits: \( \mathbb{E} \left[ \sum_{i,j} (y_i - \text{wage}_i) \right] \) subject to standard incentive compatibility and individual rationality constraints. He takes as given the parameters of the environment, which are the coefficient of absolute risk aversion of agents \( r \), the distributions of the two shocks \( \epsilon_i \) and \( \eta \), the structure of the cost function of effort and the outside option of the agents which we denote by \( \bar{v} \). The agents choose their effort levels simultaneously after learning
which wage scheme is used and what the exact parameters of that scheme are. Shocks are then realized and payments are distributed. The payment of agent $i$ is her wage minus the cost of effort: \( \text{wage}_i - e_i^2 \).

The framework described above can be extended to more than 2 agents. The extension of the IPR and the T scheme is rather straightforward, while if the RPR scheme is employed then agent $i$ gets

\[
\text{wage}_i = \hat{\alpha} + \hat{\beta} \cdot y_i + \hat{\gamma} \cdot \bar{y}_{-i}
\]

where $y_i$ is the output of agent $i$ and $\bar{y}_{-i}$ is the average output of all other agents not including agent $i$. That is, each worker receives payment in proportion $\hat{\beta}$ to his own output and in proportion $\hat{\gamma}$ to the average output of the others.

**The RPR Scheme**

The principal chooses the parameters ($\alpha$, $\beta$, $\gamma$) to maximize his expected profits given an incentive compatibility (IC) and an individual rationality (IR) constraint. Agent $i$ chooses her optimal effort level $e_i$ given the parameters of the RPR scheme. We use the approximation of expected CARA utility in terms of certainty equivalent to solve for the optimal effort level of an agent. The certainty equivalent of agent $i$ when $(e_i, e_j)$ are the effort levels chosen by agents is

\[
CE_i(e_i, e_j) = \alpha + \beta \cdot e_i + \gamma \cdot e_j - \frac{r}{2} \left[ (\beta^2 + \gamma^2) \left( \sigma_{\eta}^2 + \sigma_{\epsilon}^2 \right) + 2\beta\gamma\sigma_{\eta}^2 \right] - \frac{(e_i)^2}{c} \\
\Rightarrow e_i^* = \frac{\beta c}{2}
\]

---

10 See Tsoulouhas (2010).

11 The optimal linear RPR schemes are symmetric with respect to the agents since the principal cares about the sum of agents outputs. This is contrary to Levitt (1995), who studies optimal linear RPR schemes when the principal cares only about the highest output produced by his agents. Levitt shows that asymmetric RPR schemes sometimes do better than symmetric ones even if agents are ex-ante identical.

12 For an individual with CARA utility and normal risks, the certainty equivalent formula holds exactly. Otherwise, the relationship is approximate and we have $\mathbb{E}[u(\tilde{x})] \approx u(CE(\tilde{x})) = u(\mathbb{E}\tilde{x} - \frac{r}{2} \cdot \text{var}(\tilde{x}))$, where $\tilde{x}$ is the risky alternative, $CE(\tilde{x})$ is the certainty equivalent of $\tilde{x}$, $\mathbb{E}\tilde{x}$ is the expectation of $\tilde{x}$ and $\text{var}(\tilde{x})$ is the variance.
The principal’s maximization problem is:

$$\max_{(\alpha, \beta, \gamma)} [(1 - \beta - \gamma)E(y_i + y_j) - 2\alpha]$$

s.t. \[
\begin{align*}
e_i^* &= \frac{\beta c}{2} \quad \text{and} \quad e_j^* = \frac{\beta c}{2} \\
CE_i(e_i^*, e_j^*) &= \bar{v} \quad \text{and} \quad CE_j(e_i^*, e_j^*) = \bar{v}
\end{align*}
\]

With $\rho = \frac{\sigma^2}{\sigma^2 + \sigma^2}$, we get the optimal parameters of the RPR scheme:

$$\begin{align*}
\alpha &= \bar{v} + \frac{r}{2} \left( \beta^2 + \gamma^2 \right) \left( \sigma^2 + \sigma^2 \right) + \beta \gamma \sigma^2 \frac{\beta c}{4} - \frac{\beta \gamma c}{2} \\
\beta &= \frac{c}{c + 2r \left( \sigma^2 + \sigma^2 \right) \left( 1 - \rho^2 \right)} \\
\gamma &= -\rho \beta
\end{align*}$$

There are two features of the optimal RPR scheme that are worth noting. First, the RPR scheme partially filters out the common shock through the negative $\gamma$ coefficient: the high output produced by agent $i$ is compensated less if agent $j$ also produced a high rather than low output. Second, the behavior of agent $i$ impacts the wage received by agent $j$ and vice-versa: each unit of output produced by agent $i$ ($y_i$) lowers the wage of agent $j$ by $\rho \beta$.

In a more general case, when a principal hires more than two agents, the following two features of the optimal RPR scheme remain true: $\beta > |\gamma|$ and $\gamma < 0$. Thus, an agent who produces a high output is compensated more when the average output is low rather than high. This means that doing well when others are doing badly is better than doing well when everybody is also doing well.

To sum up, given the optimal parameters of the RPR scheme, agents choose effort levels $e_i^* = e_j^* = \frac{\beta c}{2}$ and expect a utility level of $u(\bar{v})$. The principal’s expected payoff is

$$\frac{c^2}{2c + 4r \left( \sigma^2 + \sigma^2 \right) \left( 2 \sigma^2 + 2 \sigma^2 \right)} - 2\bar{v}.$$

**The IPR Scheme**

Applying the same technique as in the RPR case, we arrive at the following optimal
parameters for the IPR scheme:

\[
\beta' = \frac{c}{c + 2r(\sigma_\epsilon^2 + \sigma_\eta^2)} \quad \text{and} \quad \alpha' = \bar{v} - \frac{(\beta')^2 c}{4} + \frac{r}{2} (\beta')^2 (\sigma_\eta^2 + \sigma_\epsilon^2)
\]

Given these parameters agents choose effort levels of \(e^*_i = e^*_j = \frac{\beta' c}{2}\) and expect a utility level of \(u(\bar{v})\). The principal’s expected payoff is \(\frac{c^2}{2c+4r(\sigma_\epsilon^2 + \sigma_\eta^2)} - 2\bar{v}\).

**The Tournament Scheme**

The optimal prize structure is\(^{13}\):

\[
W_1 = \frac{c^2 + 4Ac}{4(c + 2A^2r)} + \bar{v} \quad \text{and} \quad W_2 = \frac{c^2 - 4Ac}{4(c + 2A^2r)} + \bar{v}
\]

Given this prize structure gents choose effort levels of \(e^*_i = e^*_j = \frac{c^2}{2(c+2A^2r)}\) and expect a utility level of \(u(\bar{v})\). Principal’s expected payoff is \(\frac{c^2}{2(c+2A^2r)} - 2\bar{v}\).

**Theoretical comparison of three wage schemes**

The main feature of the RPR scheme is that the payment of agents is a function of both their absolute and relative performance. In fact, each agent receives payment in proportion to his/her output as in the IPR scheme, but is also penalized in a linear way for every unit of output produced by the other agent \((\gamma < 0)\). In an environment in which agents are risk-averse and are both subject to the common shock, the relative component of the RPR payment allows the principal to (partially) filter this common uncertainty and to balance the incentives and risk-sharing.

The combination of absolute and relative performance information in agents’ payments is what distinguishes an RPR scheme from (1) an IPR scheme, in which agents are incentivized based solely on their absolute performance and from (2) a Tournament scheme, which makes use only of the relative performance of agents. When we compare the performance of these three wage schemes for a given environment, we obtain the following results:

- The expected payoff of the principal and the effort level of agents are always higher

\(^{13}\)We concentrate on the symmetric equilibrium in which both agents exert equal effort \(e^*_1 = e^*_2\). For the detailed solution we refer the reader to Bull, Schotter and Weigelt (1987).
under the RPR scheme when compared to the IPR and the Tournament schemes.

- When the common uncertainty is high relative to the idiosyncratic one \((\sigma^2_{\eta} > 2 \cdot \sigma^2_{\epsilon})\), the Tournament gives the principal higher expected profits than the IPR scheme does. The effort of workers follows the same ordering. When the common uncertainty is small relative to the idiosyncratic one \((\sigma^2_{\eta} < 2 \cdot \sigma^2_{\epsilon})\) the IPR gives the principal higher expected profits than the Tournament scheme does. The effort of workers follows the same ordering.

4 Experiment I

In this paper we design two experiments. In Experiment 1, we test the performance of the RPR contract and compare it to the IPR and Tournament contracts both in terms of the principal’s profits and the effort levels exerted by the agents when the wage contracts are imposed on the agents. The purpose of Experiment 1 is to identify possible behavioral issues that would impact the performance of the RPR. Other-regarding preferences (such as Fehr-Schmidt (1999), Bolton-Ockenfels (2000) or Charness-Rabin (2002)) might be one possible reason for this concern; after all, each unit of output of agent \(i\) directly decreases the compensation of agent \(j\). If that’s the case, then a principal might refrain from using RPR schemes because he will end up with lower expected payoffs than if he uses other contracts like the simple piece-rate.

We test the performance of the RPR scheme in two environments: the high variance private shock (HV) (in which \(\sigma^2_{\eta} < 2 \cdot \sigma^2_{\epsilon}\)) and the low variance private shock (LV) (in which \(\sigma^2_{\eta} > 2 \cdot \sigma^2_{\epsilon}\)). In both environments we expect that under the RPR scheme the principal’s payoffs and agents’ efforts will be highest. In the HV environment we expect the IPR to dominate the T. We expect the opposite in the LV environment. These expectations from Experiment 1 are summarized in the hypotheses below:

4.1 Hypotheses

**Hypothesis 1:** The ordering of the effort levels’ the agents choose is RPR > IPR > T in the HV environment. In the LV environment this ordering is RPR > T > IPR.
Moreover, for any given contract, agents choose higher effort levels in the LV than in HV environment.

**Hypothesis 2:** In both the HV and the LV environments principal’s payoff is the highest when the RPR contract is used that when the T or the IPR contracts are used.

### 4.2 Procedures

In this section we describe the details of Experiment 1. All sessions were run at the experimental lab of the Center for Experimental Social Science (CESS) at New York University. Students were recruited from the general undergraduate population via e-mail solicitations. All sessions were conducted through computer terminals, and the software was written in Z-Tree (see Fischbacher (2007)).

Each recruited subject participated in only one session: 184 subjects participated in the Experiment 1. In each experimental session, the subjects experienced only one of the three wage schemes (IPR, T or RPR). Each session was organized according to a within subject block design: each subject went through 20 rounds of the HV environment, followed by 20 rounds of the LV environment, and then again 20 rounds of the HV environment and 20 rounds of LV (HLHL).\(^\text{14}\) For each wage scheme we also conducted a LHLH session to check for order effect and found none.\(^\text{15}\) The within-subject design allows us to study whether the subjects individually respond to an exogenous change in the environment they face and adjust their behavior accordingly.

In the HV environment, the private shock was drawn from a uniform distribution on the interval \([-24, 24]\). In the LV environment, the private shock was drawn from \(U[-14, 14]\). The variance of the common shock was kept constant in both environments and was drawn from a uniform distribution on the interval \([-27, 27]\). The cost parameter was fixed at \(c = 110\), the outside option was held constant for all environments and con-

\(^\text{14}\)Recall that HV means that the variance of the private shock was high relative to the common shock, whereas LV variance treatment means that variance of the private shock was low relative to the common shock.

\(^\text{15}\)A Kolmogorov-Smirnov test for equalities of distributions on the average effort choice for each subject shows no pair-wise difference between sessions for a given game and stage (all p-values are greater than .1). The summary statistics in Table 2, where the LHLH session was Session III for the IPR and RPR and Session IV for the T show that in terms of means these sessions are similar to the HLHL sessions, and that the direction of change between treatments is in line with that found for the HLHL sessions. In the remainder of the paper, data is pooled across sessions and regressions are clustered at the session-level.
tracts at level $\bar{v} = 7$ and the risk aversion parameter $r$ was set to 0.1.\textsuperscript{16} Table 1 displays the optimal contracts as well as the theoretical predictions for the effort levels of the agents and the expected profits of the principals for these parameters.

<table>
<thead>
<tr>
<th>Contract</th>
<th>Parameters</th>
<th>Effort Level</th>
<th>Principal’s Profit</th>
</tr>
</thead>
<tbody>
<tr>
<td>HV environment</td>
<td>RPR $\text{wage}_i = 13.63 + 0.65 \cdot y_i - 0.36 \cdot y_j$</td>
<td>35.75</td>
<td>23.62</td>
</tr>
<tr>
<td></td>
<td>IPR $\text{wage}_i = 4.21 + 0.56y_i$</td>
<td>30.80</td>
<td>18.68</td>
</tr>
<tr>
<td></td>
<td>T $W_1 = 31.16$ and $W_2 = 7.71$</td>
<td>26.87</td>
<td>14.87</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Contract</th>
<th>Parameters</th>
<th>Effort Level</th>
<th>Principal’s Profit</th>
</tr>
</thead>
<tbody>
<tr>
<td>LV environment</td>
<td>RPR $\text{wage}_i = 20.75 + 0.82 \cdot y_i - 0.65 \cdot y_j$</td>
<td>45.10</td>
<td>33.36</td>
</tr>
<tr>
<td></td>
<td>IPR $\text{wage}_i = 1.04 + 0.64 \cdot y_i$</td>
<td>35.20</td>
<td>23.26</td>
</tr>
<tr>
<td></td>
<td>T $W_1 = 36.66$ and $W_2 = 15.95$</td>
<td>40.55</td>
<td>28.55</td>
</tr>
</tbody>
</table>

Table 1: Parameters of the RPR, IPR and T contracts

In each round of Experiment 1 subjects went through the following stages: at the beginning of a round, subjects were reminded the payment structure (IPR, T or RPR) as well as the environment that they were facing (high or low private shock variance). They were randomly and anonymously matched into pairs. Subjects then had to choose an effort level and could choose any number between 0 and 55, with at most a 2 decimal point precision.\textsuperscript{17,18} After everyone made their choice, the subjects were shown their output, as well as the output of the person they were paired with, and finally the number of tokens they earned for that round. In our experiment, subjects were not given any information on their "partner’s" choice of effort, only on the output. This parallels the information available to a principal in a moral hazard context. The subjects then moved to the next round, and were re-matched with another participant.\textsuperscript{19} At the end

\textsuperscript{16}When computing the optimal parameters in each wage scheme, the principal takes $\bar{v}$ as given and ensures that in expectation the agents receive $\bar{v}$, as detailed in Section 3. In the laboratory experiment, subjects did not have an explicit outside option.

\textsuperscript{17}We restricted the effort level to be between 0 and 55 because implementing risk-aversion requires that the support of the wage be bounded. The upper limit of 55 was chosen so the theoretically optimal effort levels would not be obvious focal points.

\textsuperscript{18}Prior experimental finding suggest that the choice of bounds by the experimenter may impact the choices made by subjects in the laboratory. For example in the BDM mechanism, Bohn, Linden and Sonnegard (1997) show that in some circumstances, the higher the upper bound, the higher the average reservation price. In our experiment, the range of possible choices for effort remains constant over all schemes. Unless there is reason to believe that this would have an asymmetric effect across the different wage schemes, this rule out that these bounds explain the difference in our subjects’ choices across payment schemes.

\textsuperscript{19}Subjects were matched anonymously and randomly after each choice of effort level. So, while two
of the session, one round for each block was randomly chosen (four rounds in total), and
the tokens the students earned for that round were then converted into a probability
of winning a big prize of $4. So subjects could win up to $16 if they won in all four
blocks, and could win $0 if they did not win any of the big prizes.\textsuperscript{20} In addition, subjects
received a participation fee of $5. Each session lasted about 90 minutes, and at the end
we asked subjects to fill out a questionnaire in which we asked them questions about
themselves, their understanding of the game and how they made their choices during the
experiment.\textsuperscript{21} On average, subjects earned slightly over $20, including the participation
fee.\textsuperscript{22} The instructions for the RPR treatment are in Appendix A.

The design of Experiment 1 has four important properties:

\begin{itemize}
  \item We fix the environment (defined by the distributions of private and common shocks,
the risk aversion parameter of the agents, the costs of effort and the outside option)
and test the three wage schemes with the optimal parameters for that environment.
This allows the comparison of the relative efficiency of wage schemes both in terms
of the principal’s payoffs and in terms of how well agents target the theoretically
predicted effort levels.
  \item We use a within subject design to study each wage scheme separately (and therefore
can look at individual responses to changes in the environment), and a between
subject design to compare across wage schemes.
  \item We induce risk aversion. We induced CARA utility with risk aversion coefficient
of 0.1 using the method of Berg, Daley, Dickhaut, and O’Brien (1986) and Roth
and Malouf (1979).\textsuperscript{23} The general procedure is the following: subjects play for
tokens, and those tokens are converted into a probability of winning a big prize.

The conversion procedure converts the tokens to reflect the preferences that the

\textsuperscript{20}Since subjects were not aware of what was to happen in the next parts of the experiment, this
procedure is identical to the original procedure of inducing risk-aversion with two prizes. Indeed, in each
block, subjects could win either big prize of $4 or small prize of $0.

\textsuperscript{21}Aside from the questions pertaining to the game itself, the questionnaire also asked for a subject’s
major and year but did not ask for a subject’s gender.

\textsuperscript{22}Thus, subjects earned slightly over 13 dollars an hour, well exceeding minimum wage earnings in
New York ($7.25/hour), which is common practice for laboratory experiments.

\textsuperscript{23}Estimations of CARA coefficients have generally been between 0.0085 and 0.14 - see Saha, Shumway
and Talpaz (1994) (page 175) who summarize studies on risk aversion estimations.
experimenter would like to induce. For example, if the experimenter wants to induce risk neutrality, he/she would make the conversion linear. For risk-aversion, the conversion would be concave thus making earlier tokens more valuable. Since we induce a specific risk-aversion, we are able to use the optimal coefficients in each of the wage schemes.\(^{24}\)

- We keep the common shock as part of the environment for each wage scheme. The common shock is part of the payment for the RPR and the IPR schemes; it is, thus, not an option to remove it from these treatments. We keep it for the Tournament treatment as well for two reasons. The first is behavioral: the magnitude of the common uncertainty could be important in practice. The second is to keep the information subjects receive at each round identical across all wage schemes.\(^{25}\)

4.3 Results

We organize results from Experiment 1 around the hypotheses formulated in Section 4.1.

HYPOTHESIS 1 “Effort levels of the workers”

The effort levels chosen by agents is the main concern of the principal as it is the major determinant of output and profits. We start by discussing whether the effort levels chosen by laboratory subjects correspond to the theoretically predicted ones and obey the ordering predicted by theory.

Figure 1(a) (1(b)) show the average effort per period across all subjects in HV (LV) environment. The data from blocks of the same environment are appended at the point shown by the vertical line. The theoretical levels for each wage scheme are indicated by the horizontal dashed lines.

\(^{24}\)This method of inducing risk attitude is not uncontroversial. While some papers find that risk-averse subjects tend to behave as expected value maximizers (see, for example, Berg, Daley, Dickhaut and O’Brien (1986), Prasnikar (1993, 2002) and Rietz (1993)), others have found that this method does not change the behavior of subjects (see Walker, Smith and Cox (1990), Cox and Oaxaca (1995), or Selten, Sadrieh and Abbink (1999)). It is important to note that under risk neutrality, all wage schemes collapse and become identical in terms of profits for the principal. Thus, if subjects had behaved in a risk-neutral way in our experiments, this would have led to results opposite to those in the data, which we present in section 4.3. In the present paper it is clear that subjects behaved far from risk-neutrality.

\(^{25}\)Most experimental papers that study the tournament scheme leave the common shock out of the game as it theoretically has no impact (see Bull, Schotter and Weigelt (1987)). Wu and Roe (2005) and Wu, Roe and Sporleder (2006) are the only papers that include the common shock in tournament experiments.
In the first few rounds of the experiment the average effort per period is similar in all three wage schemes. However, as more rounds are played, the average efforts become distinct across schemes. In the experimental literature, it is a common observation that subjects take time to get used to a game and understand its mechanism. Our experiment is not an exception. For that reason we restrict our statistical analysis to the last 20 rounds of each environment.

In our analysis we will present results from both random effects regressions clustering at the session level as well as non-parametric tests using session-level averages.

In Table 2 we report the average efforts of the subjects for each scheme by session as well as the theoretical levels as predicted by the theory. In Table 3 we report the results of the Wilcoxon rank-sum test that tests whether the observed effort levels in different wage schemes come from populations with the same distribution. This comparison is of special importance since it allows us to see which of the three contracts elicits the higher effort levels from agents.

Theoretically, we expect the following rankings of the effort levels: RPR > IPR > T in the HV environment and RPR > T > IPR in the LV environment. The main prediction is borne out: in both environments, the RPR scheme elicits higher effort levels than the IPR or the T schemes. The IPR scheme performs better than T in both environments.\footnote{This result is not surprising given Figure 2 where we see that laboratory subjects drastically undershoot effort levels in the Tournament scheme, which theoretically should outperform the IPR in LV environment.}

A Random Effects regression, clustering at the session level supports the same con-
Table 2: Session-level average effort by variance.

<table>
<thead>
<tr>
<th></th>
<th>High Variance</th>
<th>Low Variance</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Data</td>
<td>Theory</td>
</tr>
<tr>
<td>IPR</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Session I</td>
<td>33.78</td>
<td>35.34</td>
</tr>
<tr>
<td>Session II</td>
<td>31.88</td>
<td>36.49</td>
</tr>
<tr>
<td>Session III</td>
<td>29.07</td>
<td>32.28</td>
</tr>
<tr>
<td>RPR</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Session I</td>
<td>38.79</td>
<td>40.98</td>
</tr>
<tr>
<td>Session II</td>
<td>35.59</td>
<td>38.76</td>
</tr>
<tr>
<td>Session III</td>
<td>36.52</td>
<td>38.66</td>
</tr>
<tr>
<td>T</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Session I</td>
<td>23.54</td>
<td>24.51</td>
</tr>
<tr>
<td>Session II</td>
<td>28.35</td>
<td>26.88</td>
</tr>
<tr>
<td>Session III</td>
<td>26.02</td>
<td>25.58</td>
</tr>
<tr>
<td>Session IV</td>
<td>24.21</td>
<td>24.71</td>
</tr>
</tbody>
</table>

Conclusions: in both environment (high and low variance), the RPR scheme elicits higher effort levels than both the IPR and T schemes. The results of this regression are in Table 4.

The behavior we observe in the Tournament scheme in the Low Variance treatment is surprising and unexpected. It is theoretically precisely in situations where the uncertainty is predominantly common that the Tournament should be advantageous. However, we observe no such thing: instead, subjects exert the least effort relative to the other schemes. At the population level, there is no statistical difference in behavior across treatments. However, this masks important individual differences in behavior that may explain what is going on. As can be seen in Figure 2, a majority of subjects in the Tournament scheme do respond to the incentives in the correct direction, that is, increase their effort when the private uncertainty is low relative to the common one (i.e. in the Low Variance treatment). However, those that do not decrease their choices by so much that the overall average stays relatively stable. There are, in fact, stark differences between the types of choices of those who did not react to the change in environment. In
<table>
<thead>
<tr>
<th>Environment</th>
<th>Observed Effort Levels (p-value)</th>
</tr>
</thead>
<tbody>
<tr>
<td>HV</td>
<td>RPR &gt;**IPR ($p = 0.0495$)</td>
</tr>
<tr>
<td></td>
<td>RPR &gt;**T ($p = 0.0339$)</td>
</tr>
<tr>
<td></td>
<td>IPR &gt;**T ($p = 0.0339$)</td>
</tr>
<tr>
<td>LV</td>
<td>RPR &gt;**IPR ($p = 0.0495$)</td>
</tr>
<tr>
<td></td>
<td>RPR &gt;**T ($p = 0.0339$)</td>
</tr>
<tr>
<td></td>
<td>IPR &gt;**T ($p = 0.0339$)</td>
</tr>
</tbody>
</table>

>** means higher at 5% (2-sided)

Table 3: Rank-sum Tests for Effort Levels between Wage Schemes

the Tournament scheme, those who did not switch average choice all chose the minimum possible effort (zero). This “dropping out” behavior, while representing only a small percentage in our experiment, has been observed in prior literature, in a larger proportion of subjects.\(^{27}\) In the RPR scheme on the other hand, those who do not change direction are predominantly choosing very high levels of effort (on average 52.8 out of a maximum of 55).

We investigate whether subjects respond correctly to a change in incentives within each scheme and test for the overall statistical difference in effort levels between the HV and LV environments. We test the equality of matched pairs of observations (average effort in each session and treatment) using the Wilcoxon matched-pairs signed-rank test. The null hypothesis that both distributions are the same is rejected at the highest level of confidence possible with three sessions for both the RPR and the IPR scheme ($p = 0.1088$). For the T scheme, the results are not significant, but the direction of the change is correct ($p = 1$).\(^{28}\) Figure 2 below shows the fraction of subjects whose effort was higher in the LV than in the HV environment (as the theory predicts). At least half the subjects responded to the incentives in the correct direction in each scheme (50% in RPR, 67% in IPR and 61% in the Tournament).

In all schemes, an increase in effort leads to a for certain increase in cost. The increase in benefits associated with an increase in cost is difference depending on the

\(^{27}\)For example, in Schotter and Weigelt (1992), subjects who are disadvantaged in the competition (ie who have a higher marginal cost of effort) are observed to drop out of T even when in equilibrium they should not.

\(^{28}\)Random Effects regressions with clustering at the session level show similar results: for both the RPR and IPR schemes, subjects exert higher levels of effort in the LV environment (significant at the 5% level) but in the T scheme there is no treatment effect.
<table>
<thead>
<tr>
<th></th>
<th>High Variance</th>
<th>Low Variance</th>
</tr>
</thead>
<tbody>
<tr>
<td>IPR</td>
<td>$-5.76^{***}$</td>
<td>$-4.41^{***}$</td>
</tr>
<tr>
<td></td>
<td>$(1.01, 0.00)$</td>
<td>$(1.09, 0.00)$</td>
</tr>
<tr>
<td>T</td>
<td>$-12.02^{***}$</td>
<td>$-13.92^{***}$</td>
</tr>
<tr>
<td></td>
<td>$(1.47, 0.00)$</td>
<td>$(0.99, 0.00)$</td>
</tr>
<tr>
<td>Constant</td>
<td>37.58^{***}</td>
<td>39.35^{***}</td>
</tr>
<tr>
<td></td>
<td>$(0.53, 0.00)$</td>
<td>$(0.62, 0.00)$</td>
</tr>
</tbody>
</table>

R-sq=.1003
Wald $\chi^2$=88.46(pvalue=0.00)
R-sq=.1360
Wald $\chi^2$=225.88(pvalue=0.00)

Coefficient and in parenthesis: robust standard errors and p-values

$^{***}$ - significant at 1%

Nb. obs: 3,680; Nb. groups: 184; Obs per group: 20.

Table 4: Predicting effort levels: random effect regression, clustering at the session level.

scheme. The tournament is the only scheme for which an increase in effort only increases the probability of receiving a higher wage. This is contrast to the IPR and RPR schemes where an increase in effort increases one’s wage directly. This may explain our subjects’ reluctance to exert as high an effort as they should theoretically. Beyond that, it can also explain why subjects who do increase their choices do so only in less dramatic fashion (on average 4 points) compared with the IPR and the RPR (both over 7 points on average).

In other words, the tournament seems more risky: subjects for sure will incur the higher costs in they increase their efforts, but they will only receive higher wages with a certain probability.

**Finding 1.** In both environments the RPR scheme elicits higher effort choices than the IPR and the Tournament contracts do.

**HYPOTHESIS 2 “Profits of the principal”**

Hypothesis 1 questioned whether subjects target the effort levels predicted by the theory when different contracts (RPR, IPR and T) are used. We have established that
Figure 2: Direction of effort changes between the high and low variance treatments.

the RPR scheme elicits higher effort choices than the IPR or the T schemes. These effort decisions influence the final profits received by the principal via two channels: (1) the total output produced and (2) the wages that principal has to pay out. Therefore, it is not obvious what the comparison between the profits in each wage schemes will be, as higher effort levels chosen by workers may increase both the output produced and the workers’ wages.

Recall that in our experiments subjects performed only the role of workers. However, given the effort levels chosen by the workers, we can compute the profits of the principal that would have hired these workers. In Table 5 we report the average expected profits of the principal, which are calculated based on the value of the expected private and common shocks (both are zero in our parametrization).

<table>
<thead>
<tr>
<th></th>
<th>HV environment</th>
<th>LV environment</th>
</tr>
</thead>
<tbody>
<tr>
<td>RPR</td>
<td>26.11 (13.81,.44)</td>
<td>23.82 (17.40,.55)</td>
</tr>
<tr>
<td>IPR</td>
<td>19.59 (8.49,.25)</td>
<td>23.08 (6.66,.19)</td>
</tr>
<tr>
<td>T</td>
<td>12.24 (21.99,.57)</td>
<td>-1.68 (23.21,.60)</td>
</tr>
</tbody>
</table>

Table 5: Expected Profits of the Principal (st. dev., st. error)

As we show in Table 5, in both environments the principal gets higher profits when he uses the RPR than the IPR or the T contracts. To test whether these differences are significant, we use the expected profits of the principal (one observation per wage scheme per session). We perform the Wilcoxon rank-sum test that asks whether the expected
profits of the principal in different wage schemes come from populations with the same
distribution and report these results in Table 6.

<table>
<thead>
<tr>
<th>Environment</th>
<th>Expected profits of the principal (p-value)</th>
</tr>
</thead>
<tbody>
<tr>
<td>HV</td>
<td>RPR &gt;**IPR  ( (p = 0.0495) )</td>
</tr>
<tr>
<td></td>
<td>RPR &gt;**T  ( (p = 0.0339) )</td>
</tr>
<tr>
<td></td>
<td>IPR &gt;*T  ( (p = 0.0771) )</td>
</tr>
<tr>
<td>LV</td>
<td>RPR = IPR  ( (p = 0.8273) )</td>
</tr>
<tr>
<td></td>
<td>RPR &gt;**T  ( (p = 0.0339) )</td>
</tr>
<tr>
<td></td>
<td>IPR &gt;**T  ( (p = 0.0339) )</td>
</tr>
</tbody>
</table>

>** ( >* ) the profits are significantly higher at 5% (10%)

Table 6: Wilcoxon rank-sum test of expected principal’s profits

As we see in Table 6, the principal gets (weakly) higher profits when the RPR scheme
is used than when IPR or T scheme is used. In the HV environment, the rank of the wage
schemes in terms of profits is as the theory predicts. However, in the LV environment,
the IPR continues to do better than the Tournament. Given that the subjects drastically
undershoot effort predictions in the Tournament, this result is not surprising. It does
however highlight the risk a principal faces when employing the tournament: the cost to
the principal (high prize plus the low prize) is independent of the output produced by
the agents. In the case where workers produce an effort below the predicted one, the
principal still has to give out the same level of payments without being compensated for
it by a high output.

This may be a weakness of the Tournament payment scheme: in this scheme, the
principal not only bears the full cost of a negative shock, but the principal also bears
the full cost if agents deviate from theory and put in below-theoretical efforts. In this
sense, the tournament is more prone to behavioral issues than the IPR or the RPR where
agents’ wages are reduced if agents exert more effort. As far as we know, our paper is
the only to explicitly incorporate a common shock into the experimental design (previous
experiments assumed this component away since it is theoretically irrelevant to an agent’s
decision-problem). Because agents exert lower effort levels than the equilibrium prediction
(in our experiment and in others), in situations where the common uncertainty is large (as in our Low Variance treatment), the principal is more penalized from deviations since the contract he offers promises high payments to the agents. Understanding behavior of subjects in the Tournament scheme requires further research.

**Finding 2.** In both environments the RPR scheme delivers (weakly) higher profits for the principal.

## 5 Experiment II

In the previous section we have established that RPR contract performs better than IPR and T contracts as the theory predicts. In other words, our results indicate that when “forced” to use the RPR scheme, subjects perform well. There are, however, several recent studies that suggest that people may dislike competition and when given the choice would not opt into such a payment scheme. Thus, it is entirely possible that people exhibit some aversion to sorting into the RPR contracts when other alternatives are available in the labor market. We design Experiment 2 to investigate this possibility.

### 5.1 Hypotheses

In Experiment 2 subjects can self-select into one of the three schemes (RPR, IPR and T). The goal of this experiment is to test whether people have any biases against or in favor of the RPR scheme when other alternatives are available. We also test how experience affects those biases.

Theoretically, when the value of outside option is kept fixed ($\bar{v} = \text{const}$) workers

---

29 There is a growing literature that shows that some people opt out of competitive and risky environments when other alternatives are available. Morgan, Orzen and Sefton (2011) show that even when the prize is high, subjects choose to enter contest at rates much below those predicted. Niederle and Vesterlund (2007) show that women may shy away from competition; Gneezy, Leonard and List (2008) establish that culture matters in determining gender differences in competitive behavior by studying patriarchal and matrilineal societies; Booth and Nolen (2009a, 2009b) show that girls from single-sex schools are more likely to behave as boys in terms of risk-taking. Also, see Eriksson and Villeval (2009) for a comparison of choices when people self-select into different wage schemes versus when schemes are exogenously imposed. This is, however, not true of all tournaments: more recently, Cason, Masters and Sheremeta (2010) show that in tournaments in which the prize is divided in proportion to output subjects exert higher effort levels and there is less “entry aversion.”
should be indifferent between the contracts. Therefore, they should be equally likely to
select each of the three available schemes as they all guarantee the same expected utility.
We start by testing if this is indeed the case when laboratory subjects have to choose
a wage scheme without having had any experience. We then let subjects experience all
three wage schemes and again let them self-select into one of them. This last part of
Experiment 2 lets us ask whether our early sorting results depend on experience.

**Hypothesis 3:** Subjects are indifferent about which payment scheme to select into.

### 5.2 Procedures

In Experiment 2 we used the HV environment from Experiment 1 and held all the pa-
rameters of this environment fixed throughout the session. A subject participating in
Experiment 2 went through the following stages:

- **We described all three wage schemes.**

- **Stage 1:** Subjects chose which wage scheme they want to play for a single (paid)
  round.\(^{30}\)

- **Stage 2:** Subjects were forced to play 20 rounds of each scheme. They were paid
  for a single round for each of the three schemes, determined randomly.

- **Stage 3:** Subjects chose which scheme they wanted to play for 20 additional rounds.
  They were paid for a single of those 20 rounds, determined randomly.

As in Experiment 1, at the beginning of each round, subjects were randomly re-
matched. At the end of each round, subjects were told their output as well as the output
of the person they were paired with. We ran two sessions of Experiment 2. A total of 47
subjects participated.\(^{31}\)

---

\(^{30}\) If an odd number of people chose T or RPR contracts, then one random subject was “paired” twice
with the remaining person. However, he/she was paid only once as the other subjects.

\(^{31}\) The only difference between these two sessions was that in Stage 2 the order of contracts was RPR,
IPR, T for one session and IPR, RPR and T for another. There was no statistical or qualitative differences
in the behavior in the two sessions, which rules out the possibility that our results are driven by the
order of the contracts presented in Stage 2.
Stage 1 aims to observe whether subjects have an initial bias for or against the RPR scheme, while Stage 3 will show whether this initial attitude changes after subjects have experienced all three available contracts. One important feature of our design is that unlike after each round of Stage 2, subjects were given no feedback after the Stage 1, so that when they arrived at Stage 3, all subjects had the same learning experience. We believe that the decision of which scheme to play for Stage 3 was not impacted by any result from Stage 1 that could have been made more salient than those from Stage 2 since in Stage 1 a single round was played. Put differently, the only difference between Stages 1 and 3 is in the amount of the experience subjects had.

In terms of incentives, subjects could earn $4 for Stage 1, $4 for each set of 20 rounds in Stage 2, and finally another $4 for Stage 3. Thus, there was a large emphasis on Stage 1, as their single-round decision would be decisive for their payment.

5.3 Results

HYPOTHESIS 3

Recall that the value of the outside option was held fixed in all three wage schemes. Therefore, we expect that subjects will be absolutely indifferent between which contract to choose since it guarantees them the same expected utility. The choice of inexperienced subjects for Stage 1 are summarized in Table 7. As is obvious, subjects are not shying away from the RPR scheme. Indeed, more than half of them choose to participate in the RPR, giving up the tournament and IPR.

<table>
<thead>
<tr>
<th>Wage contract</th>
<th># of choices (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>RPR</td>
<td>26 (55.3%)</td>
</tr>
<tr>
<td>IPR</td>
<td>12 (25.5%)</td>
</tr>
<tr>
<td>Tournament</td>
<td>9 (19.2%)</td>
</tr>
</tbody>
</table>

Table 7: Proportion of inexperienced subjects self-selecting in each contract

Even though theoretically subjects should be indifferent between three wage contracts, the chi-square goodness of fit test rejects the hypothesis that the distribution of subjects
into schemes is \((\frac{1}{3}, \frac{1}{3}, \frac{1}{3})\) in Stage 1.

In Stage 2, subjects had an opportunity to experience all three wage schemes (20 rounds of each scheme). The data from Stage 2 allow us to check the robustness of our results from Experiment 1: subjects exert effort levels of 36.43 in the RPR, 33.16 in the IPR and 29.09 in the T scheme. These results are well in line with the theory. Thus, it seems that subjects understood the incentives of each wage scheme, as we anticipated given the results of Experiment 1.

By construction, the subjects’ expected returns from each wage scheme is equal. In the laboratory, on average, subjects responded to the wage schemes in the theoretically predicted manner. Given these two facts, we would expect to observe equal shares in each wage scheme for the Stage 3. Indeed, inexperienced subjects in Stage 1 may have been influenced by "fears" that some wage schemes are harder to understand or more difficult to do well in. After their performance in Stage 2, such fears should be mitigated. Table 8 shows us the proportion of subjects in each wage scheme.

<table>
<thead>
<tr>
<th>Stage 1</th>
<th></th>
<th>Stage 3</th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>RPR</td>
<td>IPR</td>
<td>Tournament</td>
<td>Total</td>
<td></td>
</tr>
<tr>
<td>RPR</td>
<td>17 (36.2%)</td>
<td>3 (6.4%)</td>
<td>6 (12.8%)</td>
<td>26 (55.3%)</td>
<td></td>
</tr>
<tr>
<td>IPR</td>
<td>5 (10.6%)</td>
<td>5 (10.6%)</td>
<td>2 (4.3%)</td>
<td>12 (25.5%)</td>
<td></td>
</tr>
<tr>
<td>Tournament</td>
<td>6 (12.8%)</td>
<td>1 (2.1%)</td>
<td>2 (4.3%)</td>
<td>9 (19.1%)</td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td>28 (59.6%)</td>
<td>9 (19.1%)</td>
<td>10 (21.3%)</td>
<td>47 (100%)</td>
<td></td>
</tr>
</tbody>
</table>

Table 8: Choices of wage contracts in Stages 1 and 3

The RPR scheme is the only one of the three schemes where more than half of the subjects who initially chose it chose it again: 17 out of the 26 subjects chose the RPR scheme both in the Stage 1 and in the Stage 3. For both the IPR and the Tournament, more than half of the subjects moved away from their initial choices.

**Finding 3.** Subjects do not have any initial aversion to the RPR scheme. In fact, without any experience subjects seem to choose the RPR scheme more often than IPR or the T schemes. Similarly, after experiencing all three wage schemes, subjects tend to favor the RPR scheme.
6 Discussion

Our experimental results shows that subjects do not react negatively to the RPR scheme and so it is puzzling that empirical work has shown that they are seldom used. In this section we discuss why this may be.

It is conceivable that RPR schemes are in fact more widespread, but are formulated in a way that are harder to recognize. Indeed, most empirical papers (see Section 2) have tried to look for explicit evidence of their presence and incentives may be more implicit. For example, suppose that the reason people get fired is poor relative performance. That is exactly the way the RPR scheme works when payment is defined as the probability to keep a job (as opposed to the wage as in our study). So far, the empirical work that addresses this possibility has only used data on CEO turnovers, and the conclusions of the different studies diverge.\textsuperscript{32} Another possibility is that workers are rewarded in term of their future wages and not their current one. Indeed, Devaro (2006) shows the importance of relative performance (rather than absolute performance) when managers decide who to promote. So, it may be that current wages do not fit a model where performance is compared to that of one’s peers, but that progression within a firm is. In other words, RPR may be more prevalent than what we think and what has been studied empirically.

If this is the case, our experimental results suggest that principals should incorporate RPR type schemes more explicitly in their wage contracts.

7 Conclusions

In this paper we study a moral hazard environment, in which a principal hires several workers and needs to decide how to compensate them for the output they produce. The workers are subject to two types of uncertainty: private and common. In such an environment, theory predicts that the principal should use both the absolute and relative performance of workers to balance incentives and risk. The RPR scheme is

\textsuperscript{32}Morek, Shleifer and Vishny (1989) find that turnovers of CEOs equally likely to occur in troubled and in healthy industries, suggesting that industry shocks are filtered from the dismissal decision. Jenter and Kanaan (2006) document that CEOs are significantly more likely to be dismissed from their jobs after bad industry and bad market performance.
the simplest one that does the job: an agent receives payment in proportion to his output (as in standard piece-rate schemes) but is also penalized for producing less than the average output of other agents. Although the theoretical advantage of the RPR-like schemes has been long noticed in the literature, empirical papers that study this question produced mixed results. Given the lack of established evidence in favor of the effectiveness of relative performance schemes and the natural concern that such schemes may perform worse than simper schemes like piece-rate for example (due to an aversion towards competition or because of other-regarding preferences for example), the rare use of RPR schemes may have been understandable. In this paper we take the first step in investigating the performance of RPR schemes in the controlled laboratory experiment.

We do this by conducting a controlled laboratory experiment in which we fix the environment and vary only the wage contract imposed on the agents. First, we study the performance of the RPR scheme versus two alternative schemes, the piece-rate scheme (which uses only the absolute performance) and the tournament scheme (which uses only the relative performance). Our results indicate that the RPR scheme allows a principal to elicit higher effort levels from the workers and delivers (weakly) higher profits to the principal. Second, we test how subjects sort themselves into the RPR scheme when other alternatives are available. Our results suggest that subjects do not seem to exhibit any ex-ante or ex-post dislike of the RPR scheme. To sum up, consistent with theoretical predictions, RPR scheme seems to perform well both when it is exogenously imposed on agents and when it is available for self-selection on par with other alternatives. This suggests that this scheme should be used more often.

For a survey of the literature on the dearth of RPR see Lazear and Oyer (2007).
References


Appendix A

We will present here the instructions for the RPR experiment only. The instructions for tournament and IPR schemes are similar and different only in the description of the parameters of the wage schemes and the specifics of the game.

Instructions for the RPR scheme experiment

This is an experiment in decision-making. If you follow the instructions and make good decisions, you can earn a substantial amount of money, which will be paid to you at the end of the session. The currency in this decision-making problem is called Tokens. All payoffs are denominated in this currency. At the end of the experiment your earnings in Tokens will be converted into US dollars. We will describe the conversion procedure in detail later.

The experiment consists of 80 decision rounds: four blocks of 20 identical decision rounds in each block. Before the start of each block you will be given the information that is relevant for the following 20 decision rounds of the experiment. Once the block is over (this will be clearly indicated), you will receive new information that will be relevant for the following 20 decision rounds and so on.

At the beginning of each round you will be matched with one other person participating in the experiment. The identity of the person you are paired with will never be revealed to you and the person you are paired with will never know your identity.

Your decision in each round

In each round you will perform a simple task: you will choose a number between 0 and 55 - this is called your “decision number”. Associated with each decision number is a decision cost. This cost is calculated by multiplying the decision number by itself and then dividing the result by 110. For example, say you chose decision number 10. Then your cost would be \( \frac{10 \times 10}{110} = \frac{100}{110} = 0.91 \). So the cost is calculated according to the following formula:

\[
\text{Cost} = \frac{\text{Decision number} \times \text{Decision number}}{110}
\]
To help you calculate the costs for various decision numbers, we have given you a table called “Cost Table” accompanied by a “Cost Graph”. The table and the graph represent the same thing. Here is how to read the table: in the first column there are numbers. The number in the second column is the cost associated with the number in the first column. For example, the cost of choosing 35 is 11.14. Here is how to read the graph. On the lower axis you can read the different decision numbers, and you go and read the decision cost associated with that number on the vertical axis. For example, if you choose 44, the cost is 17.6.

<table>
<thead>
<tr>
<th>Decision Number</th>
<th>Cost</th>
<th>Decision Number</th>
<th>Cost</th>
<th>Decision Number</th>
<th>Cost</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0.00</td>
<td>19</td>
<td>3.28</td>
<td>38</td>
<td>13.13</td>
</tr>
<tr>
<td>1</td>
<td>0.01</td>
<td>20</td>
<td>3.64</td>
<td>39</td>
<td>13.83</td>
</tr>
<tr>
<td>2</td>
<td>0.04</td>
<td>21</td>
<td>4.01</td>
<td>40</td>
<td>14.55</td>
</tr>
<tr>
<td>3</td>
<td>0.08</td>
<td>22</td>
<td>4.40</td>
<td>41</td>
<td>15.28</td>
</tr>
<tr>
<td>4</td>
<td>0.15</td>
<td>23</td>
<td>4.81</td>
<td>42</td>
<td>16.04</td>
</tr>
<tr>
<td>5</td>
<td>0.23</td>
<td>24</td>
<td>5.24</td>
<td>43</td>
<td>16.81</td>
</tr>
<tr>
<td>6</td>
<td>0.33</td>
<td>25</td>
<td>5.68</td>
<td>44</td>
<td>17.60</td>
</tr>
<tr>
<td>7</td>
<td>0.45</td>
<td>26</td>
<td>6.15</td>
<td>45</td>
<td>18.41</td>
</tr>
<tr>
<td>8</td>
<td>0.58</td>
<td>27</td>
<td>6.63</td>
<td>46</td>
<td>19.24</td>
</tr>
<tr>
<td>9</td>
<td>0.74</td>
<td>28</td>
<td>7.13</td>
<td>47</td>
<td>20.08</td>
</tr>
<tr>
<td>10</td>
<td>0.91</td>
<td>29</td>
<td>7.65</td>
<td>48</td>
<td>20.95</td>
</tr>
<tr>
<td>11</td>
<td>1.10</td>
<td>30</td>
<td>8.18</td>
<td>49</td>
<td>21.83</td>
</tr>
<tr>
<td>12</td>
<td>1.31</td>
<td>31</td>
<td>8.74</td>
<td>50</td>
<td>22.73</td>
</tr>
<tr>
<td>13</td>
<td>1.54</td>
<td>32</td>
<td>9.31</td>
<td>51</td>
<td>23.65</td>
</tr>
<tr>
<td>14</td>
<td>1.78</td>
<td>33</td>
<td>9.90</td>
<td>52</td>
<td>24.58</td>
</tr>
<tr>
<td>15</td>
<td>2.05</td>
<td>34</td>
<td>10.51</td>
<td>53</td>
<td>25.54</td>
</tr>
<tr>
<td>16</td>
<td>2.33</td>
<td>35</td>
<td>11.14</td>
<td>54</td>
<td>26.51</td>
</tr>
<tr>
<td>17</td>
<td>2.63</td>
<td>36</td>
<td>11.78</td>
<td>55</td>
<td>27.50</td>
</tr>
<tr>
<td>18</td>
<td>2.95</td>
<td>37</td>
<td>12.45</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

So, in each round you choose a decision number, then simply enter it into the box on the screen and push the “continue” button. The person you are paired with will also choose his decision number. You can choose any number between 0 and 55, but it has to be a number with no more than one digit after the decimal point. For example, 26
and 41.2 are valid entries while 15.55 is not. Also, note that you will not get to see what choice anyone else has made.

You will have 20 seconds to choose your decision number.

**Payoff in each round**

After both you and the person you are paired with have entered your decision numbers, the computer will select three numbers, lets call these $n$, $s$ and $j$.

- $j$ is a number that the computer will choose at random, and can be anything between $-27$ and $27$, with each number having equal chances of being picked.

- $n$ and $s$ are also numbers that the computer will choose at random. The range in which they will be chosen will change for each block. You will be told what that range is at the beginning of each block, again each number having equal chances of being picked. The computer will choose $n$ and $s$ randomly and independently of each other.

Note that the values that the computer will pick at each round for $n$, $s$ and $j$ are independent of the previous values that were chosen. We will call your decision number $+n+j$ your outcome. The outcome of the person your are paired with is his/her decision number $+s+j$. Note that the number $j$ appears in both expressions. So, for a particular round, you and the person you are paired with have the same value for $j$.

For the first block you will receive tokens according to the following formula (this will appear on the screen):

$$20.75 + 0.82 \times \text{Your Outcome} - 0.65 \times \text{Outcome of other person} - \text{Cost of your Decision Number}$$

The other person you are paired with will receive tokens according to the following
formula:

\[ 20.75 + 0.82 \times \text{His/Her Outcome} - 0.65 \times \text{Your Outcome} - \text{Cost of His/Her Decision Number} \]

After both you and the person you are paired with have made your decisions, you will observe your outcome and the outcome of the person you are paired with. You will also see how many tokens you have earned for that round. Then you will move on to the next round. Here is an example that is not meant to be realistic.

- Suppose that you choose a decision number equal to 8.
- Suppose in addition that the person you are paired with also chose a decision number equal to 8.
- In addition, let's suppose that \( n = -10 \), \( s = 7 \) and \( j = -12 \). In this case, your outcome is \( 8 - 10 - 12 = -14 \) and your cost is \( \frac{8 \times 8}{110} = \frac{64}{110} = 0.58 \) (you can also read this from the Cost Table or Graph). The outcome of the other person is \( 8 + 7 - 12 = 3 \) and his/her cost is \( \frac{8 \times 8}{110} = 0.58 \).

So you get \( 20.75 + 0.82 \times (-14) - 0.65 \times (3) - 0.58 = 6.74 \) tokens. The person you are paired with gets \( 20.75 + 0.82 \times 3 - 0.65 \times (-14) - 0.58 = 13.53 \) tokens.

To summarize:

- The number of tokens you earn in each round depends on your selected decision number (both because it plays a role in determining your outcome, and because it enters as a cost and reduces the amount of tokens you get by (decision number \( \times \) decision number)/110). The number of tokens to earn in each round also depends on the “outcome” of the person you are paired with.
- For each block you will be told the range in which \( n \) and \( s \) can be chosen.
- For each block we will change the numbers in the formula that determines the amount of tokens you and the person you are paired with get at each round.
• After you and the person you are paired with have chosen your decision numbers, and after the computer randomly chose \( n, j \) and \( s \), you will see both your and the other person’s outcomes. You will also see the amount of tokens you have earned for this round. Then you will be randomly re-matched with someone and will move on to the next round.

**How Tokens are Converted into Money**

Your payment for the experiment is described here. You can earn money for each of the four blocks, but note that you will only be paid at the very end of the session.

Whether you get money in a particular block depends on a lottery which has two prizes: a big prize of 4 dollars, and a small prize of zero. For each block the computer will choose one decision round to “count”. The amount of tokens you won for this round will be converted into a probability that tells you how likely you are to win the big prize. We have given you a sheet of paper called “Information for Block I” with a graph on it (see Figure 3 below). Here is how to read the graph: if you take a number on the horizontal axis (that’s the axis that is lying left to right) and draw a vertical line to the point where it crosses the curved line and then go read what number that corresponds to on the vertical axis (that’s the axis going top to bottom) you can read the percentage chance of winning the big prize. So, for example, say you won \(-30\) tokens for the round that was chosen. This means that you have about 55 out of 100 chances of getting the large prize of four dollars, whereas if you had earned zero tokens you would have had about 95 out of 100 chances of winning the four dollars. A negative number of tokens in a round does not mean that you are losing tokens. It also does not mean that you are having no chance of winning the big prize of four dollars. It’s just that the smaller the amount of tokens per round, the smaller the chances of winning the big prize, and a negative number is smaller than a positive one. The precise conversion is given by the graph. If you do not win the four dollars, you win zero dollars. The graph starts at \(-40.17\) tokens on the horizontal axis because this is the least amount of tokens you can earn in a round, and it goes up to 64.41 because this is the most tokens you can earn in a round. The general procedure for converting tokens to the probability of winning the big prize is the same in all four block. However, the particular conversion will change at
each block. So we will be handing out new graphs at the beginning of each block, and this graph will be relevant for that block only.

![Figure 3: Probability of winning big prize.](image)

We will follow this procedure for each block. So you can win up to $16 if you win the lottery for each block, and you can also win $0 if you do not win the lottery for any of the blocks. In addition to this you will receive a $5 show up fee.
Information for Block I

• The number \( j \) can be any number between \(-27\) and \(27\).

• The numbers \( n \) and \( s \) can be any number between \(-14\) and \(14\).

• In each round for this block:

\[
\text{Tokens for you} = 20.75 + 0.82 \times \text{“Your outcome”} \\
- 0.65 \times \text{“Outcome of other person”} \\
- \text{“Cost of your decision number”}
\]

\[
\text{Tokens for other person} = 20.75 + 0.82 \times \text{“His/her outcome”} \\
- 0.65 \times \text{“Your outcome”} \\
- \text{“Cost of his/her decision number”}
\]

“Your outcome” = Your decision number + \( n + j \)

“Outcome of other person” = His/her decision number + \( s + j \)

• Conversion of tokens you earned into the probability of winning the big prize in this block is according to the new graph (see picture below)